Analysis of microarray data with pathway information

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The newest research center of Ecole des Mines

Started in 2002, became an autonomous research center in 2006

Objective: develop mathematical approaches and computational tools to process and analyze biological and chemical data

http://cbio.ensmp.fr
1. **Machine learning and statistics** (theory and algorithms)
2. **Analysis of post-genomic data and systems biology** (focus on cancer and malaria)
3. **Data analysis methods for new technologies** (DNA chips, cell chips, high-throughput microscopy)
4. **Virtual screening** (docking, ligand-based)
Outline

1. Classification and interpretation of microarray data
2. Including pathway information
Classical setting

Data available
- Gene expression measures for more than 10k genes
- Measured on less than 100 samples of two (or more) different classes (e.g., different tumors)

Goal
- Design a classifier to automatically assign a class to future samples from their expression profile
- Interpret biologically the differences between the classes
Classical setting

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The approach

- Each sample is represented by a vector \( x = (x_1, \ldots, x_p) \) where \( p > 10^5 \) is the number of probes.
- **Classification**: given the set of labeled sample, learn a linear decision function:

\[
    f(x) = \sum_{i=1}^{p} \beta_i x_i + \beta_0,
\]

that is positive for one class, negative for the other.
- **Interpretation**: the weight \( \beta_i \) quantifies the influence of gene \( i \) for the classification.
Linear classifiers

Pitfalls

- No robust estimation procedure exist for 100 samples in $10^5$ dimensions!
- It is necessary to reduce the complexity of the problem with prior knowledge.
Example: Norm Constraints

The approach

A common method in statistics to learn with few samples in high dimension is to constrain the norm of $\beta$, e.g.:

- Euclidean norm (support vector machines, ridge regression): $\| \beta \|_2 = \sum_{i=1}^{p} \beta_i^2$
- $L_1$-norm (lasso regression): $\| \beta \|_1 = \sum_{i=1}^{p} |\beta_i|$

Pros
- Good performance in classification

Cons
- Limited interpretation (small weights)
- No prior biological knowledge
### Example 2: Feature Selection

#### The approach

Constrain most weights to be 0, i.e., select a few genes (< 20) whose expression are enough for classification. Interpretation is then about the selected genes.

#### Pros
- Good performance in classification
- Useful for biomarker selection
- Apparently easy interpretation

#### Cons
- The gene selection process is usually not robust
- Wrong interpretation is the rule (too much correlation between genes)
Motivation

- Basic biological functions are usually expressed in terms of **pathways** and not of single genes (metabolic, signaling, regulatory)
- Many pathways are already known
- How to use this prior knowledge to constrain the weights to have an interpretation at the level of pathways?
Pathway interpretation

The graph is the complete known metabolic network of the budding yeast (from KEGG database).

We project the classifier weight learned by a SVM.

Good classification accuracy, but no possible interpretation!
Pathway interpretation

Good example

- The graph is the complete known metabolic network of the budding yeast (from KEGG database).
- We project the classifier weight learned by a spectral SVM.
- Good classification accuracy, and good interpretation!
Pre-process each microarray profile to filter out the high frequencies with respect to the known pathways. This involves discrete Fourier transforms + spectral graph theory.

Perform classical SVM on the smoothed expression profiles.
You will always have an interpretable model because you enforce it. Can we trust it?

- Any method must use prior knowledge because of the $n \ll p$ problem.
- In many cases the “true” classifier is more likely to have a pathway interpretation than to be based on a few genes only.

There are many cases where smoothness is not expected on the pathway (negative regulation...)

- We just enforce a global smoothness, local jumps are possible (although penalized).
- As more data are available, a more precise estimation is possible.
Conclusion

- Manipulating gene expression data is difficult for statistical reasons.
- Inclusion of prior knowledge is required (e.g., feature selection)
- Known pathways form a natural prior knowledge
- This results in classifiers with good accuracy and interpretability.
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