

# Efficient remote homology detection using local structure

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#### **ABSTRACT**

Motivation: The function of an unknown biological sequence can often be accurately inferred if we are able to map this unknown sequence to its corresponding homologous family. At present, discriminative methods such as SVM-Fisher and SVM-pairwise, which combine support vector machine (SVM) and sequence similarity, are recognized as the most accurate methods, with SVM-pairwise being the most accurate. However, these methods typically encode sequence information into their feature vectors and ignore the structure information. They are also computationally inefficient. Based on these observations, we present an alternative method for SVM-based protein classification. Our proposed method, SVM-I-sites, utilizes structure similarity for remote homology detection.

**Result:** We run experiments on the Structural Classification of Proteins 1.53 data set. The results show that SVM-I-sites is more efficient than SVM-pairwise. Further, we find that SVM-I-sites outperforms sequence-based methods such as PSI-BLAST, SAM, and SVM-Fisher while achieving a comparable performance with SVM-pairwise.

**Availability:** I-sites server is accessible through the web at http://www.bioinfo.rpi.edu. Programs are available upon request for academics. Licensing agreements are available for commercial interests. The framework of encoding local structure into feature vector is available upon request.

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#### INTRODUCTION

Proper identification of homologous relationships in proteins is important in advancing our understanding of the functions of biological sequences. Much research has been focused on protein homology detection. Dynamic programming based alignment tools such as Smith–Waterman (Smith and Waterman, 1981) and their efficient approximations such as BLAST (Altschul *et al.*, 1990) and FASTA (Pearson, 1985) have been widely used to provide evidence for homology by matching a new sequence against a database of previously

annotated sequences. However, these approaches can only detect homologous proteins that exhibit significant sequence similarity.

In order to identify weak or remote homologies, one can utilize the concept of protein family or superfamily, which represents a group of sequences sharing the same evolutionary origin. A statistical model can be built for each family or superfamily, and a new sequence is subsequently compared with these models. In contrast to simple pairwise comparison methods, the ability to match a sequence to superfamilybased models computationally allows biologists to infer nearly three times as many homologies (Park et al., 1998). Profiles (Gribskov et al., 1987) and hidden Markov models (Krogh et al., 1994; Baldi et al., 1994) are two methods commonly used for representing these models. These probabilistic models are often called generative because the methodology involves building a model for a single protein family and then evaluating each candidate sequence to see how well it fits the model. If the 'fit' is above some threshold, then the protein is classified as belonging to the family.

By gleaning the extra information of unlabelled protein sequences in large databases, iterative methods such as PSI-BLAST (Altschul *et al.*, 1997) and SAM (Karplus *et al.*, 1998) improve upon profile-based methods by iteratively collecting homologous sequences from a large database and incorporating the resulting statistics into a central model.

A recently proposed approach called the discriminative method is able to attain additional accuracy by modelling the difference between positive and negative examples explicitly. There are two steps in this approach: a given set of proteins is first converted into fixed-length vectors, before an SVM is trained from the vectorized proteins. The most prominent works that employ this approach include SVM-Fisher (Jaakkola *et al.*, 2000) and SVM-pairwise (Li and Noble, 2003). The two methods differ mainly in the vectorization step. In SVM-Fisher, a protein's vector representation is its gradient with respect to a profile hidden Markov model; while in SVM-pairwise, the vector is a list of pairwise sequence similarity scores. While the SVM-pairwise method

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is currently the most accurate method for detecting remote homologies, it is inefficient and not scalable.

All the above works detect remote homology using only sequence information. This is accurate only if the proteins are closely related. In this paper, we offer an efficient vectorization method while maintaining a comparable performance with SVM-pairwise. We encode structure information into feature vectors instead of using sequence similarity for remote homology detection. Here, we assume that the structure information is given by the probability that the protein contains certain local structure, as predicted by a library of sequence-structure motifs I-sites library (Bystroff and Baker, 1998). Experimental results on SCOP1.53 databases demonstrate that the accuracy of our proposed method is comparable with the state-of-the-art method SVM-pairwise and outperforms methods such as PSI-BLAST, SAM and SVM-Fisher.

#### SYSTEM AND METHODS

#### Overview

Figure 1 gives the overview of the proposed SVM-I-sites method. It consists of two phases: (a) the training phase which constructs support vector classifiers, and (b) the testing phase which uses a support vector machine (SVM) to determine if the protein belongs to some known protein classes. Both phases require the extraction of features from the proteins and represent them in some suitable form. The form of representation essentially distinguishes SVM-I-sites from SVM-Fisher and SVM-pairwise. SVM-Fisher and SVM-pairwise represent a protein's vector using sequence information. In contrast, SVM-I-sites encode the local structure information into a feature vector. This allows us to incorporate a natural biological interpretation into our method to capture parts of the 'signature' of the protein's three-dimension structure.

During the training phase, the proteins in the database are transformed into high-dimensional feature vectors. These feature vectors are separated into two classes, namely, positive and negative examples. An SVM is subsequently constructed to discriminate the positive and negative examples. This process is repeated for all protein classes under investigation. The output from the training phase is a set of SVM, one for each protein class.

In the testing phase, a high-dimensional feature vector is created for the protein under investigation. Each of the trained SVM is then queried to determine whether the given protein belongs to the particular protein class associated with the SVM. A positive result would suggest that the protein under investigation has a homologous relationship with the corresponding protein class.

#### Feature extraction and representation

While sequence information provides important hints to the presence of homologous relationship, we observe that a large

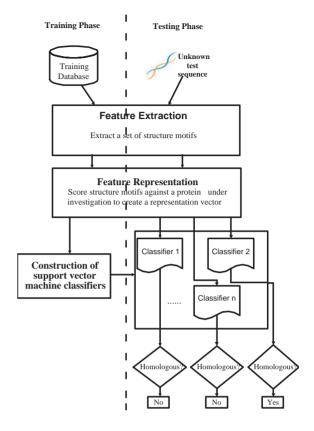


Fig. 1. Overview of SVM-I-sites.

number of remote homologous proteins have sequences that are weakly similar. Instead, their three-dimensional structures share many common characteristics. The most straightforward way to incorporate structure information in remote homology detection is to encode them into the features. Unfortunately, three-dimensional protein structures cannot be accurately predicted from sequences.

An intermediate but useful step is to predict the protein secondary structure, by projecting the complicated three-dimensional structure onto one dimension, i.e. onto a string of secondary structural assignments for each residue. Sequences which are distantly related to each other but which have similar functions, tend to have highly conserved patterns of secondary structure (Russell *et al.*, 1994). A better one-dimensional representation of proteins is the generalized 'local structure', which includes two of the three secondary structure types (helix and strand) but reclassifies the loop states to one of several different loop types, such as the Schellman cap motif shown in Figure 2. These loop motifs often have specific sequence signatures that are conserved between remote homologs.

Pioneering work in protein secondary structure prediction includes (Efimov, 1993; Hutchinson and Thornton, 1994; Zhu and Blundell, 1996; Oliva *et al.*, 1997; Han *et al.*, 1996). However, the majority of these methods do not identify the strong

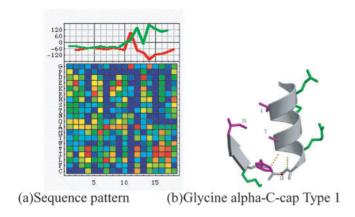


Fig. 2. This is one of the sequence profiles and its corresponding local structure in I-sites library. (a) The sequence pattern for Glycine alpha-C-cap Type 1. Along the Y-axis are the 20 amino acids, arranged roughly from non-polar on the bottom to polar on the top, except that glycine and proline are on the top and cystine is on the bottom. Along the X-axis is the position in the motif, each column represents one amino acid. The different color represents frequency of occurrence: red for high frequency (log-odds ratio > 3), and blue for low frequency (log-odds ratio < -3). (b) The three-dimensional element which has a strong correlation with the sequence patterns of (a). In the Type 1 glycine cap, an amphipathic helix is followed immediately by a glycine and an aspartate beta-bend. The aspartate is preferred in the position two residues after the glycine. Conserved non-polar sidechains 1 and 4 residues after the glycine interact with two conserved non-polar sidechains 4 and 7 residues before the glycine.

relationship between the amino acid sequence and structure. Further, the focus of these methods is on the three-state secondary structure prediction, namely helix, stand and loop. Hence, they are not suitable for encoding secondary structure information into feature vectors.

One of the most successful local structure prediction methods is by Bystroff and Baker (Bystroff and Baker, 1998), which performs local structure prediction based on a library (I-sites library) of short sequence patterns (profiles) that correlate strongly with protein three-dimensional structure elements. In the I-sites library, there are 263 sequence-structure profiles each of which corresponds to a unique structure motif which are more specific than the three-state secondary structure. Figure 2 is an example of sequence-structure profile.

In order to predict the local structure of any unknown protein sequence, the sequence patterns (profiles) for each of the 263 clusters of I-sites library are used to score all subfragments of this unknown target sequence. Given the length difference, the similarity scores of different clusters are not directly comparable. Instead the associated 'confidence' values are compared. The confidence of a fragment prediction is the probability that a sequence segment with a given score has the predicted structure. Each cluster has a confidence curve

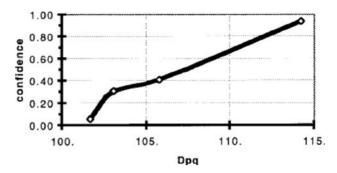


Fig. 3. A confidence curve map similarity score to confidence.

(Fig. 3) which maps similarity score to the probability of correct local structure based on a ten-fold jack-knife test: 90% of the database is used to refine each of the cluster, while the remaining 10% is set aside for scoring the profile of this cluster. The top-scoring segments are kept. The structures of the top-scoring segments are then compared to the paradigm structure for the cluster, chosen from the 90% training set. The list is sorted by score and the fraction of true-positive in the cluster. This procedure is repeated 10 times using a different 10% as the test set and the results are averaged. Please refer to (Bystroff and Baker, 1998) for the details of the confidence curve generation procedure.

Given any protein sequence, we use the following method to obtain its structure features: the first step is to run PSI-BLAST against swissprot database to generate a multiple sequence alignment. After that, the multiple alignment is converted to a sequence profile, and the sequence profile is searched in overlapping windows using each of the 263 I-sites and we get a score for each sub-fragment. Finally, each score is translated into a probability ('confidence') value, and the whole set of 'confidence' values are sorted. Thus, for each sub-fragment, we obtain the probability ('confidence' value) of this subsequence belonging to each of the 263 structure motifs.

To minimize the effect due to mutation, we apply a threshold such that if the 'confidence' value falls below the threshold, then the confidence of this subsequence will be set to zero. The number 0.25 is the default value of I-sites program. Initial experiments show that using a threshold of 0.5 gives the best performance. Details of the experiments are given in experimental results section.

Several heuristics can be used to handle the situation where a protein motif occurs many times. For example, we can take the maximum, the sum, or the average of all the 'confidence' value for such protein motifs. Initial experiments to determine a good heuristics show that using the sum value gives the best performance. Details of the experiment are given in experimental results section. Table 1 shows a sample of the vector generated for the protein d9atcb2. Each feature value in the vector denotes the sum 'confidence' value of the corresponding local structure occurring in the protein.

Table 1. A sample of the generated structure feature values

Local structure	Feature value
	4.76
	3.84
	4.23

It is possible that two(or more) overlapping subsequences show similarity to different I-site motifs. At the same time, many of I-site motifs tend to overlap. This may cause one single subsequence to yield high confidence value to multiple different motifs. In this paper, we keep all the predictions even when there exists some overlap. In future, we shall look into some appropriate overlap removing algorithm to improve the performance.

#### Construction of SVM classifiers

Having obtained the feature vectors for the proteins, the next step is to predict whether the given feature vector exhibits homologous relationship with any of the known protein families. Classical machine learning techniques such as Naive Bayes classifiers (Lanley *et al.*, 1992), neural networks (Pao, 1989), decision tree classifiers (Quinlan, 1993) etc. do not perform well for remote homology detection because they are unable to effectively obtain good generalization from sparse training data in high dimensions.

The well-established SVM exhibits excellent generalization performance in practice and is grounded in statistical learning theory (Vapnik, 1998). SVM locates a hyperplane that maximizes the distance separation between the positive and negative examples. Figure 4 shows the two-dimensional case.

We first train the SVM to find the optimal partitioning hyperplane. Next, SVM will predict the classification of an unknown protein by mapping it into the feature space and determining which side of the hyperplane the unknown protein lies on.

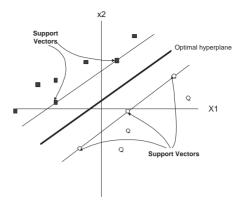


Fig. 4. Support vector machines.

In our implementation, we use the *Gist* SVM software implemented by Noble and Pavlidis (Noble and Pavlidis, 2002, www.cs.columbia.edu/compbio/svm). It contains a kernel function that acts as the similarity score between pairs of input vectors. The base kernel is normalized so that each vector has length 1 in the feature space, i.e.,  $K(X,Y) = (X \cdot Y)/\sqrt{(X \cdot X)(Y \cdot Y)}$ . The parameters needed to tune a SVM are the 'capacity' and the choice of kernel. The former controls the error tolerance in the classification of training samples. This affects the generalization ability of the SVM and prevents overfitting. In our experiments, we set capacity to be 10, which guarantees sufficient generalization and the numerical stability of SVM.

The kernel function allows the SVM to create hyperplanes in high dimensional spaces that effectively separate the training data. In the input space, training vectors are often not separated by a simple hyperplane. The kernel maps data from one space to another such that a simple hyperplane can effectively separate the data into two classes. We employ the Gaussian kernel for all the classifiers. The variance of the associated Gaussian Kernel is computed as the median Euclidean distance (in feature space) from any positive training examples to the nearest negative example. The output is a discriminant score that is used to rank the members of the test set.

To determine whether an unlabelled protein belongs to a particular protein class, we test it against the SVM trained for that class. The SVM classifier produces a 'score' representing the distance of the testing feature vector from the margin. The larger the score is, the further away the vector is from the margin, and the more confident we are of the classifier's prediction.

### **COST ANALYSIS**

Computational efficiency is an important characteristic for any homology detection algorithm. In this respect, SVM-I-sites method is more efficient than SVM-pairwise. Both SVM-I-sites and SVM-pairwise include an SVM optimization and vectorization step. In the optimization step, both algorithms take  $O(n^2)$  time, where n is the number of training set

examples. The vectorization step of SVM-pairwise involves computing  $n^2$  pairwise scores. Using Smith-Waterman, each computation takes  $O(m^2)$ , yielding a total running time of  $O(n^2m^2)$ , where m is the length of the longest training set sequence.

In contrast, SVM-I-sites first runs PSI-BLAST to obtain a profile before it runs I-sites function to compute the 'confidence' value of each sequence containing a pre-defined local structure. The time complexity of running PSI-BLAST on the swissprot database is O(N) when the length of the query sequence k is much less than N, where N is the size of the swissprot database. The time complexity of running I-sites function is O(k) for each sequence. Hence, the total running time of SVM-I-sites is O(nN). Since N is typically an order of m\*n where m is a two order number, we conclude that SVM-I-sites is about one order faster than SVM-pairwise.

We also carry out an experiment to compare the response time of SVM-pairwise and SVM-I-sites for the vectorization step. The time taken by SVM-pairwise includes the CPU time and the output time of the  $n^2$  pairwise scores, while the time taken by SVM-I-sites includes the CPU time and output time of PSI-BLAST and I-sites function. This experiment is performed on a Pentium III 750 MHz Ultra Sparc running SunOS 5.8 with 8 GB RAM. I-sites takes 19 h, and the Smith–Waterman algorithm requires 70 h. Clearly, SVM-I-sites is four times faster than SVM-pairwise in vectorization step. Note that the real-time comparison is not as significant as the theoretical analysis because the number of I/Os incurred by SVM-I-sites is much more than that for SVM-pairwise.

## **PERFORMANCE STUDY**

In this section, we compare the performance of SVM-I-sites, PSI-BLAST, SAM, SVM-Fisher and SVM-pairwise. We evaluate the accuracy of each algorithm by its ability to classify protein domains into superfamilies in the Structural Classification of Proteins (SCOP) (Murzin *et al.*, 1995) version 1.53. Sequences are selected using the Astral database [astral.stanford.edu (Brenner *et al.*, 2000), and similar sequences are removed using an *E*-value threshold of  $10^{-25}$ ]. This procedure resulted in 4352 distinct sequences, grouped into families and superfamilies. The database is selected so as to provide a direct comparison with previous work on remote homology detection method, namely, SVM-pairwise.

We use the same experimental setup as SVM-pairwise. For each family, the protein domains within a family are considered positive test examples; while the protein domains outside the family but within the same superfamily are taken as positive training examples. The data set yields 54 families containing at least five family members (positive test) and 10 superfamily members outside of the family (positive train). Negative examples are taken from outside of the

positive sequences' fold, and are randomly split into train and test sets in the same ratio as the positive examples.

## **Comparative methods**

The vectorization step of SVM-pairwise uses the Smith–Waterman algorithm as implemented on the BioXLP hardware accelerator (www.cgen.com). The feature vector corresponding to protein X is  $F_X = f_{x1}, f_{x2}, \ldots, f_{xn}$ , where n is the total number of proteins in the training set and  $f_{xi}$  is the E-value of the Smith–Waterman score between sequence X and the ith training set sequence. The default parameters are used: gap opening penalty and extension penalties of 11 and 1, respectively, and the BLOSUM 62 matrix.

For comparison, we also include the result of PSI-BLAST, SAM and SVM-Fisher methods presented in the SVM-pairwise paper (Li and Noble, 2003). The SAM method trains the Hidden Markov models using the Sequence Alignment and Modeling toolkit (Krogh *et al.*, 1994). Models are built from unaligned positive training set sequences using the local scoring option ('–SW 2'). Each of the test sequences is compared to the model by using *hmmscore* together with the local scoring option. The resulting *E*-values are used to rank the test set sequences.

The SVM-Fisher method uses the same trained HMMs during the vectorization step. Forward and backward matrices are combined to yield an observation count for each parameter in the HMM. As in (Jaakkola *et al.*, 2000), the counts can be converted into components of a gradient vector. Although the gradient components can be computed for every HMM parameter, the SVM-Fisher method uses only the gradient components that correspond to emission probabilities in the match states. Further, a compact gradient vector can be derived using a mixture decomposition of the emission probabilities. For a profile HMM containing *m* match states, the length of the resulting vector is 9*m*.

In PSI-BLAST, the input is a single sequence, whereas for methods such as HMMER and SVM-Fisher, the input consists of multiple input sequences. In our experiments, we randomly select a positive training set sequence to serve as the initial query. The complete positive training set is aligned using CLUSTALW (Thompson *et al.*, 1994). Then the query sequence and the alignment is used as inputs. We run one iteration of PSI-BLAST with the test set as a database. Note that PSI-BLAST is not run on the test set for multiple iterations: this restriction allows a fair comparison with the other, non-iterative methods included in the study. The resulting *E*-values are used to rank the test set sequences.

Note that the setup of SAM and PSI-BLAST methods as presented in SVM-pairwise is slightly different from their commonly reported usuage (Park *et al.*, 1998). It is possible for SAM, PSI-BLAST and SVM-Fisher to achieve better performance than those reported here if they have the benefit of putative homologs from large sequence databases as (Park *et al.*, 1998).

Function compute\_medianRFP\_score

Input: SVM scores of the positve test sequences

and negative test sequences

Output: Median RFP score

- 1. Sort the SVM scores of the positive test sequences
- 2. Compute the median of the SVM score of the positive test sequences
- 3. Median RFP=ratio of negative test sequences which score above or equal to the median value

Fig. 5. Algorithm to compute median RFP score.

```
Function compute ROC score
Input: SVM scores of the positve test sequences
negative test sequences
Output: ROC score
Sort the SVM scores of the test sequences and
get a sorted list of class labels (1 or -1) in a single
column
tp=0
       /* Initialize true positive */
fp=0 /* Initialize false positive */
roc=0 /* Initialize ROC score
for each of the sorted label do
 if (label=1) then tp=tp+1
  else {
     fp=fp+1
    roc=roc+tp}
if (tp=0) then roc=0
else if (fp=0) then roc=1
   else roc=roc/(tp*fp)
```

Fig. 6. Algorithm to compute ROC score.

### **Performance metrics**

We use the two scoring methods as reported in SVM-pairwise (Li and Noble, 2003) to compare these methods, namely, the receiver operating characteristic (ROC) scores, and median rate of false positives (RFP). The ROC score is the area under the receiver operating characteristic curve—the plot of true positives as a function of false positives (Gribskov and Robinson, 1996). A score of 1 indicates perfect separation of positives from negatives, whereas a score of 0 denotes that none of the sequences selected by the algorithm is positive. The algorithm to compute ROC score is shown in Figure 6. The median RFP score is the fraction of negative test sequences that score as high or better than the median-scoring positive test sequence. The algorithm to compute median RFP score is shown in Figure 5.

Table 2. Results of the experiments to determine the best heuristics

Heuristic methods	Average ROC score for the 54 SCOP families
Maximum	0.88
Sum	0.89
Average	0.86

Table 3. Results of the experiments to determine the best threshold

Thresholds	Average ROC score for the 54 SCOP famili
0.25	0.89
0.4	0.89
0.5	0.90
0.6	0.88

## **Experimental results**

Table 2 summarizes the average ROC score for 54 SCOP families using different heuristics to account for multiple subsequence occurrences at default threshold 0.25. Table 2 shows that the sum heuristics gives the best performance.

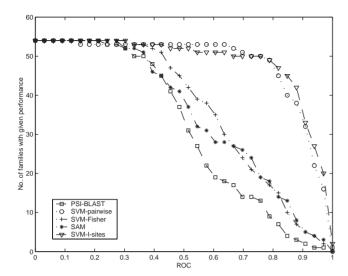
Table 3 shows the average ROC score for 54 SCOP families using different thresholds and sum to account for multiple subsequence occurrences. From Table 3, we see that threshold 0.5 gives the best performance. The final performance is a combination of 0.5 threshold and sum to account for multiple subsequence occurrences.

The results of the comparative experiment are given in Figures 7 and 8. The two graphs rank the five homology detection methods according to ROC and median RFP scores. Each series corresponds to one protein homology detection method and a higher curve corresponds to more accurate homology detection performance. We observe that SVM-I-sites performs significantly better than PSI-BLAST, SAM and SVM-Fisher methods, and is comparable to SVM-pairwise. This is because SVM-pairwise adopt pairwise scores as feature values and the Smith–Waterman algorithm is the most sensitive pairwise comparison method.

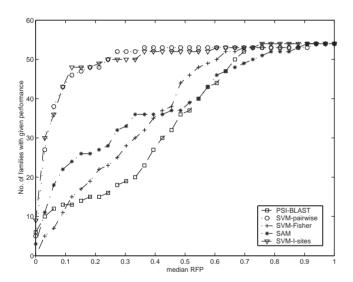
SVM-I-sites can be an alternative and complimentary method to SVM-pairwise method to construct features with local structure probabilities. This can be shown from Figures 7 and 8. Figure 9 is a family-by-family comparison of the 54 ROC scores computed for each method. The results suggest that SVM-I-sites and SVM-pairwise are two complimentary methods for detection of remote homology.

#### DISCUSSION

The inference of homology relationship in proteins with known structure and/or function is a core problem in computational biology. Sequence comparison is the most commonly



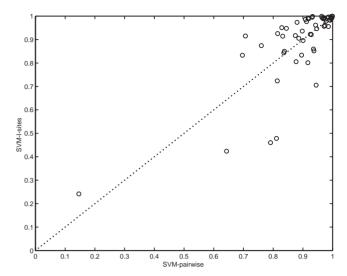
**Fig. 7.** Relative performance of homology detection methods. The graph plots the total number of families for which a given method exceeds a ROC score threshold.



**Fig. 8.** Relative performance of homology detection methods. The graph plots the total number of families for which a given method exceeds a median RFP score threshold.

used approach to determine homology. However, remote homologous proteins tend to have little sequence similarities. As such, they are often statistically undetectable using conventional sequence comparison methods. Homology or common ancestry in such cases needs to be inferred from their common three-dimensional structures and functions.

The main novelty of our work is in investigating how local structure information can help remote homology detection. By using local structure features, we seek to develop an approach that has a natural biological interpretation. Further, we have described an integrated framework to construct



**Fig. 9.** Family-by-family comparison of SVM-pairwise and SVM-I-sites. Each point on the graph corresponds to one of the 54 SCOP superfamilies. The axes are ROC scores achieved by the two primary methods compared in this study: SVM-pairwise and SVM-I-sites.

feature vectors that encode structure information. The local structure is encoded into the feature vector so that parts of the three-dimensional 'signature' is captured. The use of SVMs also enables learning to take place in high dimensional feature space. Our experiment results confirm that it is important to incorporate structure information in the feature space.

Efficiency is another advantage of SVM-I-sites compared to SVM-pairwise. SVM-I-sites is more efficient in the vectorization step, thus making it a more practical solution for large databases.

In addition, SVM-I-sites method shares many advantages as SVM-pairwise. First, it does away with the need for profile HMM topology and parametrization. Second, it learns from both positive and negative training examples, while a profile method is trained solely on a collection of positive examples. Third, it does not require a multiple alignment of the training set sequence which may not be possible for distantly related protein sequences.

Current work ignores the local structure order. This may result in proteins containing the same local structure but with different orders being classified into the same superfamily. Ongoing work includes investigating how the local structure order influence the remote homology detection performance.

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