

Uncovering transcriptional regulation of metabolism by using metabolic network topology

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Cellular response to genetic and environmental perturbations is often reflected and/or mediated through changes in the metabolism, because the latter plays a key role in providing Gibbs free energy and precursors for biosynthesis. Such metabolic changes are often exerted through transcriptional changes induced by complex regulatory mechanisms coordinating the activity of different metabolic pathways. It is difficult to map such global transcriptional responses by using traditional methods, because many genes in the metabolic network have relatively small changes at their transcription level. We therefore developed an algorithm that is based on hypothesis-driven data analysis to uncover the transcriptional regulatory architecture of metabolic networks. By using information on the metabolic network topology from genome-scale metabolic reconstruction, we show that it is possible to reveal patterns in the metabolic network that follow a common transcriptional response. Thus, the algorithm enables identification of so-called reporter metabolites (metabolites around which the most significant transcriptional changes occur) and a set of connected genes with significant and coordinated response to genetic or environmental perturbations. We find that cells respond to perturbations by changing the expression pattern of several genes involved in the specific part(s) of the metabolism in which a perturbation is introduced. These changes then are propagated through the metabolic network because of the highly connected nature of metabolism.

bioinformatics | reporter metabolites | metabolic subnetworks

Linking the genome to its functioning metabolism is of substantial interest not only in studying human diseases (1) but also for identifying metabolic engineering targets in biotechnological applications (2, 3). Transcriptional analysis represents a high-throughput and genome-wide approach for linking the set of expressed genes to functional metabolism of the cell. Indeed, several studies using genome-wide gene-expression analysis have shown that transcriptional regulation plays an important role in regulating metabolism in response to perturbations (4–6). Although many statistical methods and clustering algorithms provide tools to analyze such transcriptomics data (7–9), these methods seldom provide insight into the regulatory architecture of the metabolic networks without intelligent analysis of the results (up/down-regulation of genes of interest or correlation between genes of interest). This shortcoming is primarily due to the hypothesis that there may be all-to-all interactions among the genes being analyzed, resulting into many biologically nonsignificant results. One of the ways to address this problem is to integrate known biological interactions, e.g., protein–protein interactions, in the analysis of transcription data (10). Such an approach essentially reduces the degrees of freedom in data analysis by using knowledge of molecular interactions occurring in the cell. The organization and functioning of the cell can be viewed as a complex network of molecular interactions. These interactions are mediated not only by physical contacts between individual molecules (e.g., protein–protein and protein–DNA interactions) but also result from the functional coupling of certain molecules or groups of molecules (11). Cellular metab-

olism thus can also be viewed as a network of functional interactions between enzymes and metabolites. This metabolic network represents the channels for the flow of material and generation of Gibbs free energy, which are constrained by the conservation laws of mass and energy. Consequently, we hypothesized that the topology of the interactions involved in metabolism can be used to understand the underlying regulatory mechanisms (e.g., at transcriptional level) controlling this flow of mass and energy. To test this hypothesis, we developed an algorithm that integrates gene-expression data with topological information from genome-scale metabolic models, which enabled systematic identification of so-called reporter metabolites that represent hot spots in terms of metabolic regulation. This study was an attempt to infer the global role of a metabolite based on mRNA-expression patterns and metabolic stoichiometry without direct measurement of metabolite concentration. The algorithm also identifies the significantly correlated metabolic subnetworks after direct or indirect perturbations of the metabolism.

Algorithm

Fig. 1 schematically illustrates the proposed algorithm, which is described step by step in the following.

Graph-Theoretical Representation of the Metabolic Network. The complete metabolic network in the cell can be represented as a bipartite undirected graph, here referred to as a metabolic graph (Fig. 1) (also see supporting information, which is published on the PNAS web site). In this metabolic graph, metabolites as well as enzymes are represented as nodes, and interactions between them are represented as edges. Thus, a metabolite node is connected to all of the enzyme nodes that catalyze a reaction involving that particular metabolite, and an enzyme node is connected to all of the metabolites that take part in the corresponding reaction. This graph is bipartite, because neither metabolite nor enzyme nodes are directly connected among them.

We also define a unipartite undirected graph, here referred to as an enzyme (or reaction) interaction graph (Fig. 1) (also see supporting information). In this graph, only enzymes are represented as the nodes, and the two enzymes sharing a common substrate in the corresponding reactions are connected to each other. Thus, edges in this graph represent the metabolites shared by two enzymes. Some enzymes catalyze several different reactions, and these enzymes are represented by a single node. This node is linked to all enzyme nodes that are connected to the different reactions carried out by this enzyme.

Mapping and Scoring of Transcription Data. The transcriptional data used in this study can be classified into two categories. The first

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Abbreviation: KEGG, Kyoto Encyclopedia of Genes and Genomes.

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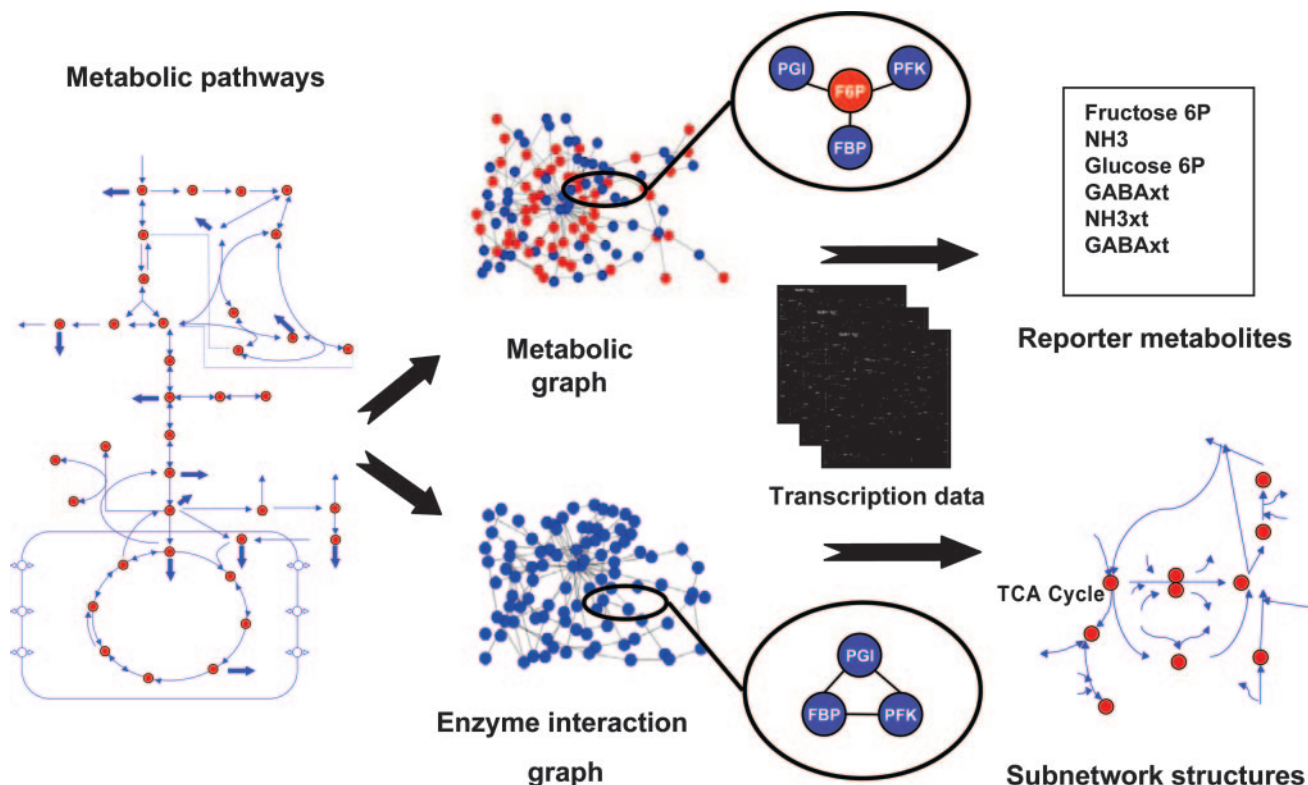


Fig. 1. Illustration of the proposed algorithm for identifying reporter metabolites and subnetwork structures signifying transcriptionally regulated modules. A metabolic network (set of reactions) is converted to bipartite (metabolic) and unipartite (enzyme-interaction) graph representations. Gene-expression data from a particular experiment then is used to identify highly regulated metabolites (reporter metabolites) and significantly correlated subnetworks in the enzyme-interaction graph.

category includes data in which two different strains (or conditions) are compared and with multiple measurements for each strain (or condition). We refer to this data type as differential data. The second category of data are multidimensional data, e.g., gene expression measured over a time course or with analysis of multiple strains, with or without multiple measurements at the same time point or strain.

Differential data can be mapped on the enzyme nodes of the metabolic or enzyme-interaction graph with a specification of the significance of differential gene expression. Here we used the student's *t* test to obtain *p* values, with p_i representing the significance of the change for each enzyme. Each p_i can subsequently be converted to a *Z* score of the enzyme node (Z_{ni}) by using the inverse normal cumulative distribution (θ^{-1}).

$$Z_{ni} = \theta^{-1}(1 - p_i)$$

In the case of multidimensional data, the absolute Pearson correlation coefficient, P_j is calculated between all pairs of nodes (enzymes) connected by an edge in the enzyme-interaction graph. The P_j of an edge can be converted to a *Z* score for that edge (Z_{ej}) by using the inverse normal cumulative distribution.

$$Z_{ej} = \theta^{-1}(P_j)$$

The *Z* score follows a standard normal distribution for random data, where *p* values or Pearson coefficients follow a uniform distribution.

Method for Identification of Reporter Metabolites. To identify the reporter metabolites, each metabolite node in the metabolic graph is scored based on the normalized transcriptional response of its neighboring enzymes. In case of differential data, the

normalized transcriptional response was calculated as size-independent aggregated *Z* scores of the *k* neighboring enzymes.

$$Z_{\text{metabolite}} = \frac{1}{\sqrt{k}} \sum Z_{ni}$$

$Z_{\text{metabolite}}$ scores can be corrected for the background distribution by subtracting the mean (μ_k) and dividing by the standard deviation (σ_k) of the aggregated *Z* scores of several sets of *k* enzymes chosen randomly from the metabolic graph.

$$Z_{\text{metabolite}}^{\text{corrected}} = \frac{(Z_{\text{metabolite}} - \mu_k)}{\sigma_k}$$

For multidimensional data, the neighboring enzymes of a metabolite in the metabolic graph are represented as an enzyme-interaction graph with all enzymes connected to each other, and hereby *Z* scores for each edge (Z_{ej}) can be calculated as described before. Subsequently, the $Z_{\text{metabolite}}$ score can be calculated and corrected for the background distribution in the same way as for differential data.

The scoring used for identifying reporter metabolites is basically a test for the null hypothesis, “neighbor enzymes of a metabolite in the metabolic graph show the observed normalized transcriptional response by chance.” The metabolites with the highest score (typically up to 10) are defined as reporter metabolites, and they mark spots in the metabolism, where there is substantial regulation either to maintain homeostasis (i.e., a constant level of the metabolite) or adjust the concentration of the metabolite to another level required for proper functioning of the metabolic network.

Table 2. Reporter metabolites for $\Delta gdh1$, $\Delta grr1$, and carbon source data sets

Metabolite	No. of neighbors	No. of KEGG pathways
$\Delta gdh1$		
Fructose 6-phosphate	15	5
Glucose 6-phosphate	11	6
NH ₃ xt	3	—
NH ₃	32	7
GABAxt	2	—
CTP	8	1
Fructose 1,6-bisphosphate	4	4
Sedoheptulose 7-phosphate	5	2
CO ₂ M	12	—
N-Acetyl-L-glutamate 5-semialdehydeM	2	—
$\Delta grr1$		
L-Glutamine	20	5
Glucose-xt	14	—
Mannose	15	2
Fructose	14	3
Fructose-xt	12	—
Glycogen	4	—
Orthophosphate	65	3
Glucose	28	6
Mannose-xt	11	—
Homocitric acid	2	2
Carbon source		
Maltose	4	1
Carnitine	3	1
(R)-Pantoate	2	1
Glyoxylate	6	5
6-phospho-gluconate	5	1
Episterol	2	—
3-Demethylubiquinone-9M	2	—
H ⁺ EXT	42	—
3-Phosphonoxypruvate	3	1
1-Phosphatidyl-1-D-myo-inositol 4-phosphate	4	2

Only the top scoring 10 metabolites are shown. Data show the number of neighbors to the reporter metabolite (or the number of reactions in which the reporter metabolite participates) and the number of KEGG pathways in which the reporter metabolite appears. The metabolite names ending with "M" and "xt" indicate that the metabolite is present in mitochondrial compartment and extracellular medium, respectively. Because KEGG pathways do not classify metabolites in this fashion, the corresponding fields in the table are empty. —, data not available.

(21). Overall, it is known that Grr1p deactivates the Rgt1p transcriptional repression of several hexose transporters, and the important role of Grr1p in regulating sugar transporters is clearly seen from the list of reporter metabolites identified in this case (Table 2). Among the 10 most important reporter metabolites, six are hexoses, all transported by the group of *HXT* genes in *S. cerevisiae*. The other reporter metabolites include glutamine, orthophosphate, and glycogen. Glutamine plays a key role in the nitrogen metabolism, which is normally considered also to be regulated by Grr1p, although a direct link has not been established (22). Orthophosphate is involved in a large number of reactions in the central carbon metabolism, and the identification of this reporter metabolite is a clear indication of the multitude of effects caused by deletion of *GRR1*. In the $\Delta grr1$ mutant, a high-scoring metabolic subnetwork of 204 genes was identified, and additional analysis of this network resulted in identification of a 52-gene subnetwork (Table 1). Besides several genes encoding sugar and amino acid transporters that are

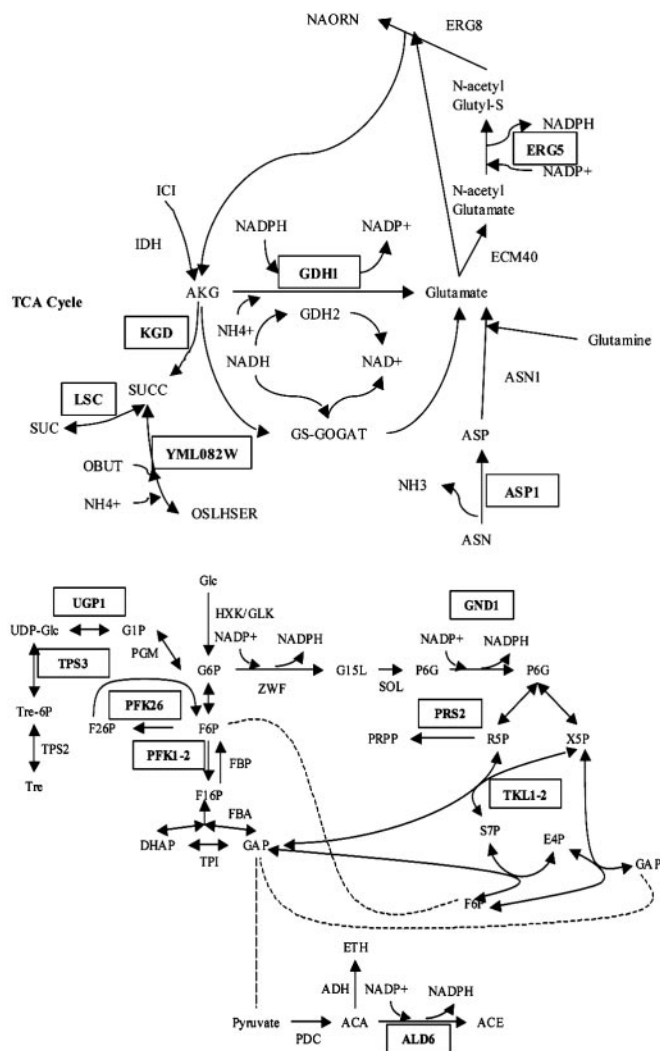


Fig. 2. Parts of *S. cerevisiae* metabolism that are represented in the subnetwork identified for the $\Delta gdh1$ data set. Genes present in the subnetwork are shown in boxes.

known to be regulated by Grr1p, this subnetwork also contains many other genes involved in amino acid metabolism.

Multidimensional Data. To illustrate the application of the method for analysis of transcription data measured over several different environmental conditions, we analyzed transcription data for *S. cerevisiae* grown on four different carbon sources, glucose (a hexose), maltose (a disaccharide), and two C-2 compounds, ethanol and acetate (23). For analysis of this type of data set, it is intuitively more difficult to interpret the results in terms of the changes in physiology, because the data span a multidimensional space. However, the reporter metabolites (Table 2) still reflect the metabolic reprogramming in response to the changes in carbon source. Maltose is an obvious reporter metabolite, because enzymes involved in uptake and metabolism of this sugar are induced only in the presence of maltose. The presence of glyoxylate and carnitine as reporter metabolites is due to the key roles of these metabolites during growth on C-2 compounds (24). Appearance of H⁺ as a reporter metabolite illustrates the ability of the algorithm to identify metabolites indirectly involved in metabolism, because transport of maltose and acetate is coupled with proton transport across the cell membrane. We also

